

1. Check how the following invariants can change by taking a minor or a contraction of the graph:
  - (a) minimum vertex cover size,
  - (b) maximum independent set size,
  - (c) minimum feedback vertex size,
  - (d) minimum dominating set size,
  - (e) maximum clique size,
  - (f) length of the longest path,
  - (g) length of the longest cycle.
2. Prove the following statement: for every  $k \geq 1$  and planar graph  $G$ , the vertices  $V(G)$  has a partition into  $k$  sets  $V_1, \dots, V_k$  such that the treewidth of  $G \setminus V_i$  has treewidth at most  $f(k)$  for some function  $f$ .
3. Is it possible to generalize Courcelle's Theorem from bounded treewidth to bounded local treewidth?
4. Design a PTAS for DOMINATING SET on planar graphs.
5. Reduce the problem of finding a cycle of length at least  $k$  to the problem of finding a cycle of length exactly  $k$ .
6. Draw a  $K_6$  on the torus (extra task: draw  $K_7$ ).